

Computer Graphics

Lecture-11

Two –Dimensional Viewing and Clipping

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Lecturer

DIIT

Liang-Barsky Algorithm

- The following parametric equations represent a line from (x_1, y_1) to (x_2, y_2) along with its infinite extension:

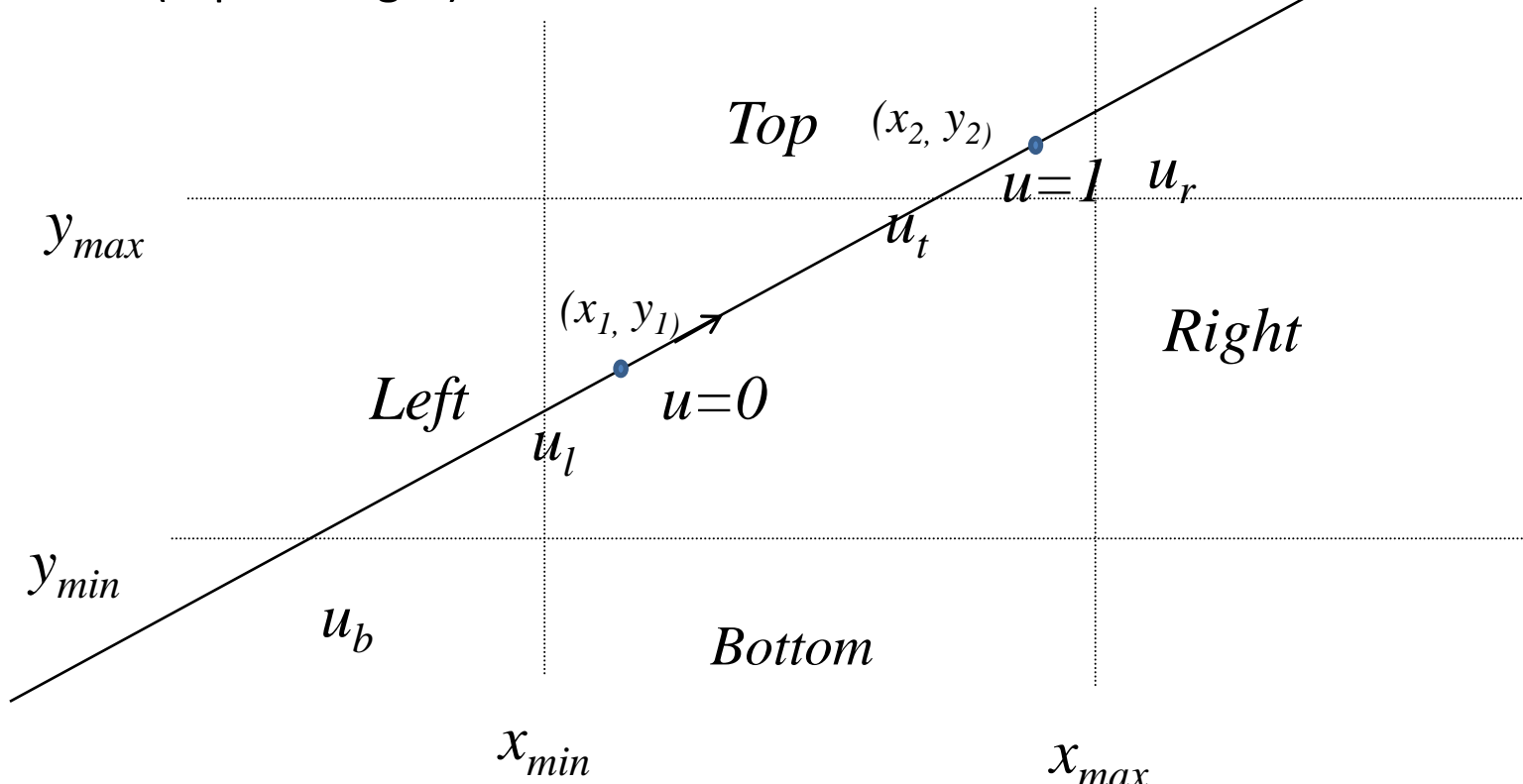
$$x = x_1 + \Delta x \cdot u$$

$$y = y_1 + \Delta y \cdot u$$

- Where $\Delta x = x_2 - x_1$
 $\Delta y = y_2 - y_1$

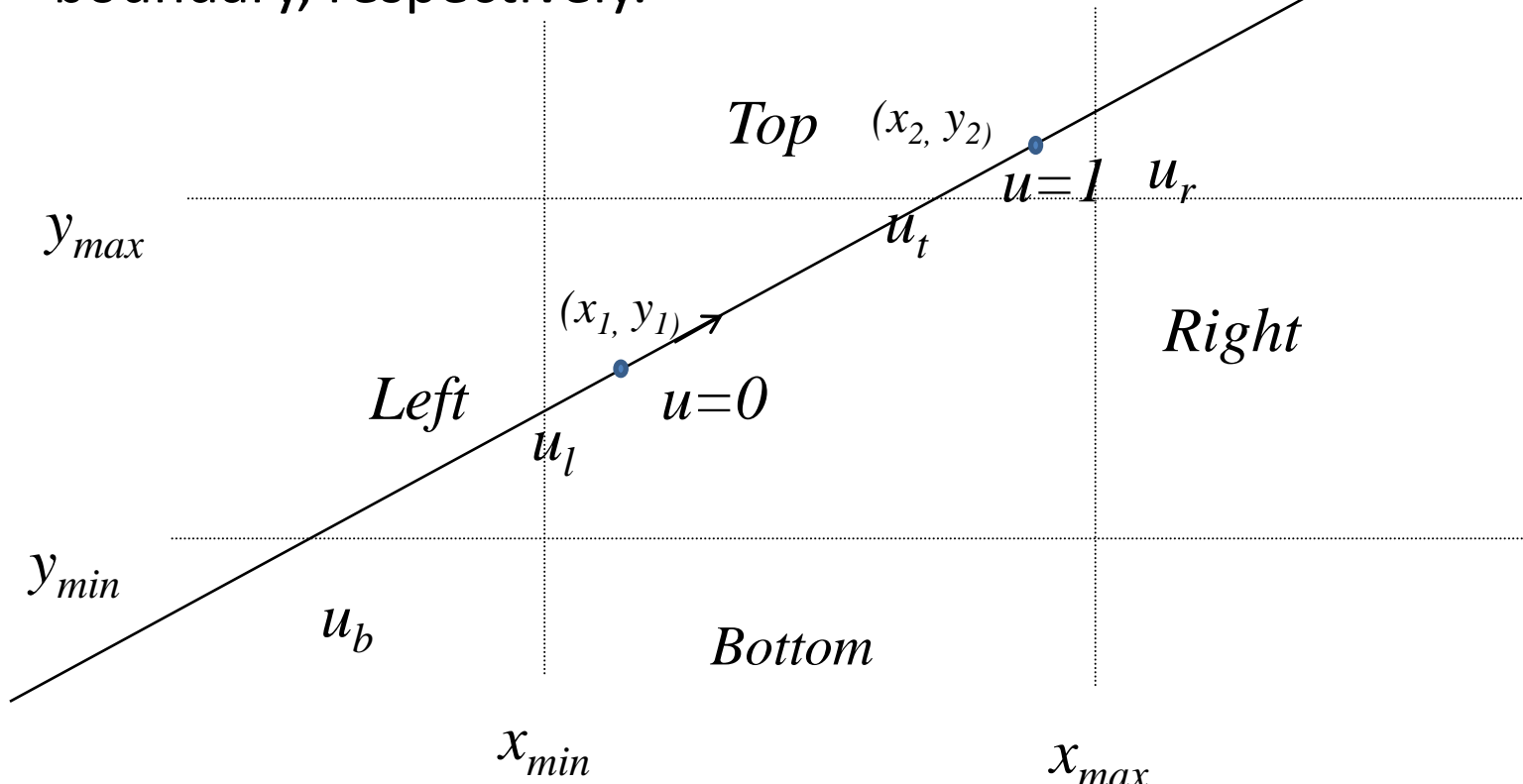
Liang-Barsky Algorithm

- The line itself corresponds to $0 \leq u \leq 1$.
- u increasing from $-\infty$ to ∞
- First move from the outside to the inside of the clipping window's two boundary lines (bottom and left)
- Then move from the inside to the outside of the other two boundary lines (top and right).

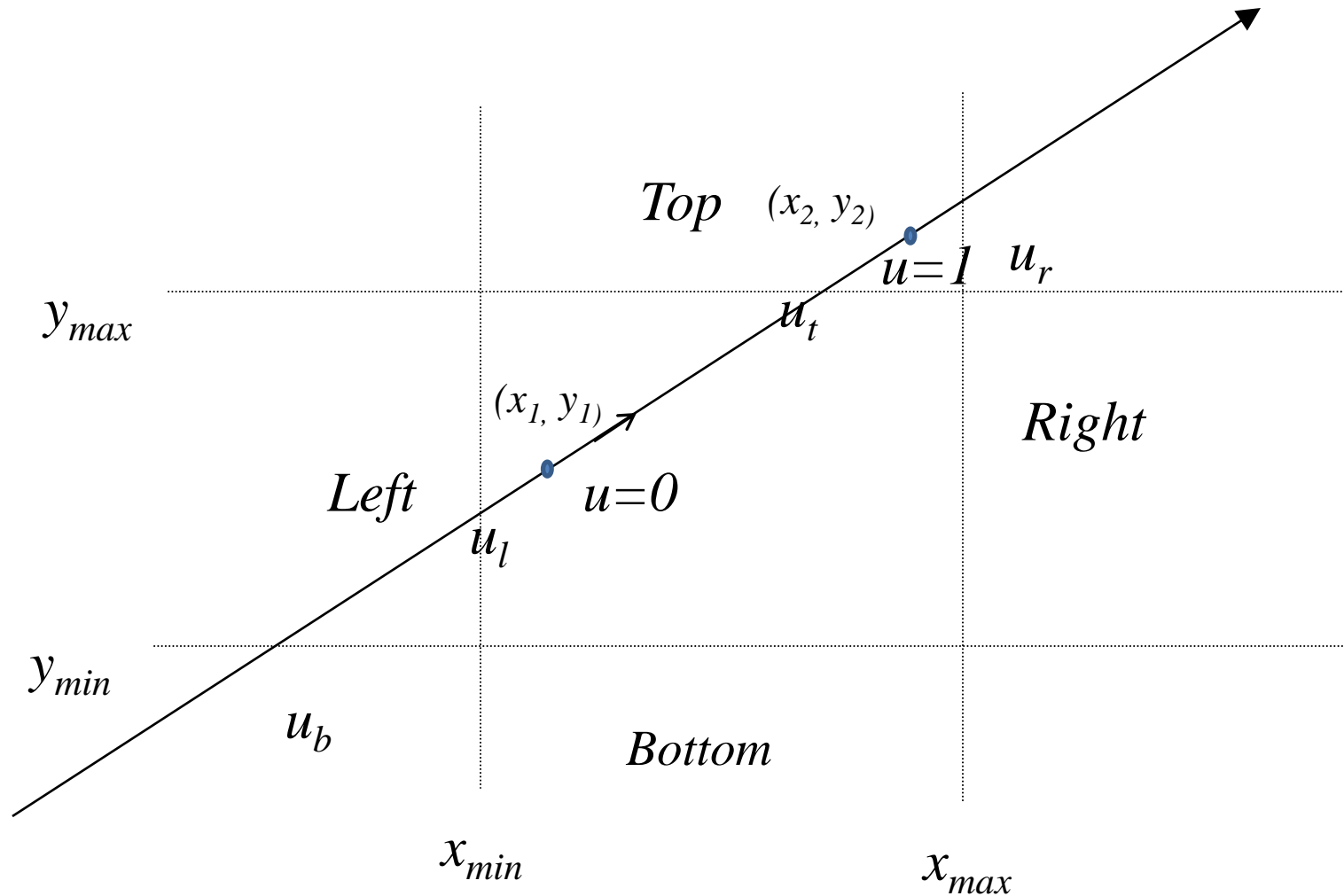


Liang-Barsky Algorithm

- $u_1 = \text{maximum}(0, u_l, u_b)$ and $u_2 = \text{minimum}(1, u_t, u_r)$
- u_l, u_b, u_t, u_r correspond to the intersection point of the extended line with the window's left, bottom, top, right boundary, respectively.



Parametric Intersection



Liang-Barsky Algorithm

- For point (x,y) inside the clipping window, we have

$$x_{\min} \leq x_1 + u\Delta x \leq x_{\max}$$

$$y_{\min} \leq y_1 + u\Delta y \leq y_{\max}$$

- Rewrite the four inequalities as

$$up_k \leq q_k, \quad k = 1, 2, 3, 4$$

- Where

$p_1 = -\Delta x,$	$q_1 = x_1 - x_{\min}$	Left
$p_2 = \Delta x,$	$q_2 = x_{\max} - x_1$	Right
$p_3 = -\Delta y,$	$q_3 = y_1 - y_{\min}$	Bottom
$p_4 = \Delta y$	$q_4 = y_{\max} - y_1$	Top

Observation

- If $p_k = 0$, the line is parallel to the corresponding boundary and
 - $q_k < 0$, the line is completely outside the boundary and can be eliminated
 - $q_k \geq 0$, the line is inside the boundary and needs further consideration,
- If $p_k < 0$, the extended line proceeds from the outside to the inside of the corresponding boundary line
- If $p_k > 0$, the extended line proceeds from the inside to the outside of the corresponding boundary line
- When $p_k \neq 0$, the value of u that corresponds to the intersection point is q_k / p_k

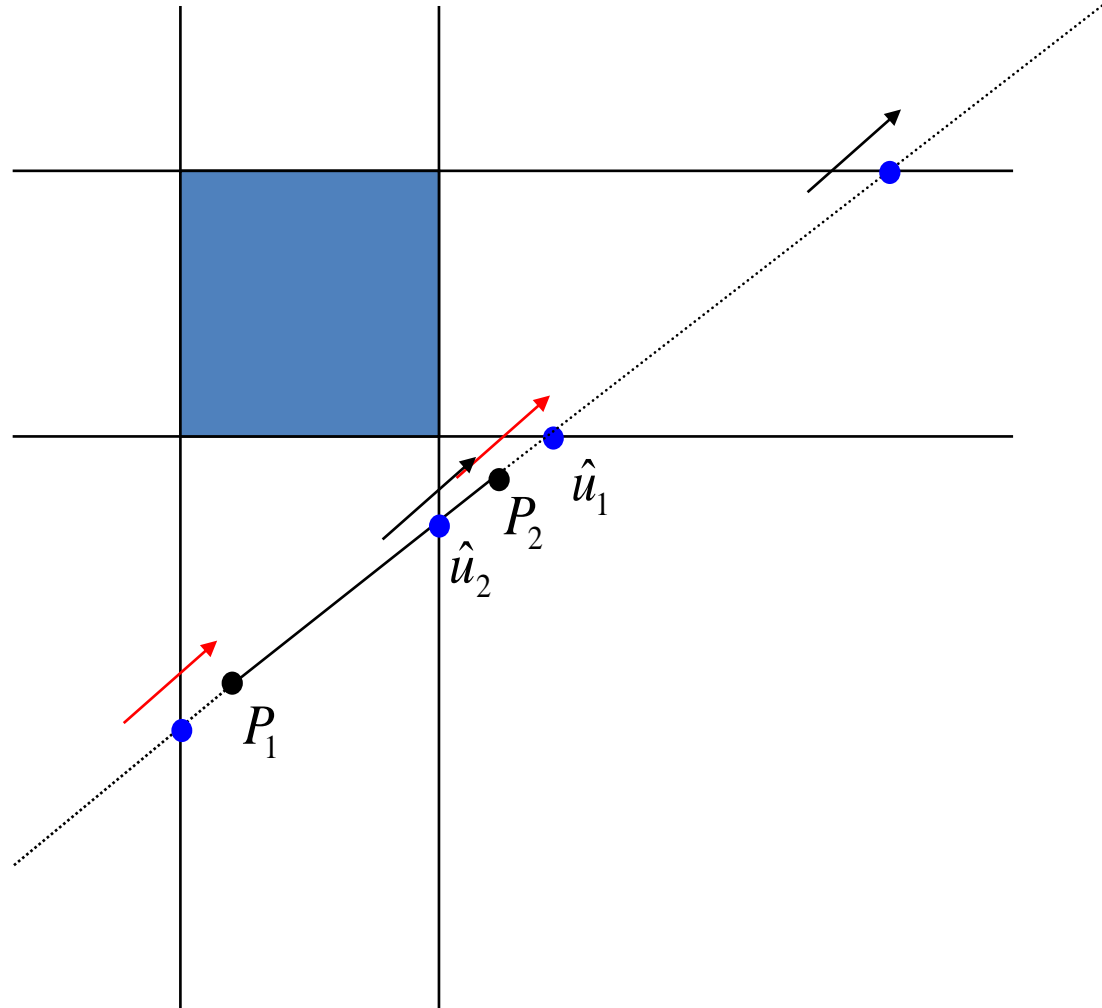
Liang-Barsky - Algorithm

- If $p_k=0$ and $q_k<0$ for any k , eliminate the line and stop. Otherwise proceed to the next step.
- For all k such that $p_k<0$, calculate $r_k = q_k/p_k$. Let u_1 be the maximum of the set containing 0 and the calculated r values.
- For all k such that $p_k>0$, calculate $r_k = q_k/p_k$. Let u_2 be the minimum of the set containing 1 and the calculated r values.
- If $u_1 > u_2$, eliminate the line since it is completely outside the clipping window. Otherwise, use u_1 and u_2 to calculate the end points of the clipped line.

Line Clipping – Liang-Barsky

- If $u_1 > u_2$, the line lies completely outside of the clipping area.
- Otherwise the segment from u_1 to u_2 lies inside the clipping window.

if $\hat{u}_1 > \hat{u}_2$, rejected.



Example

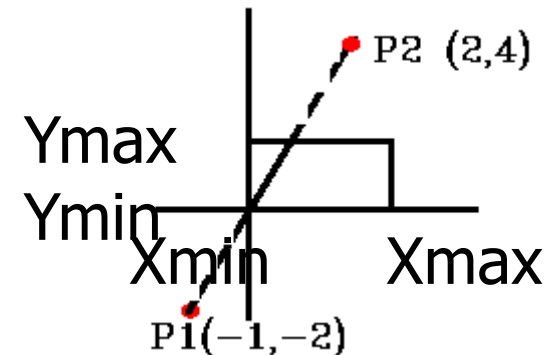
Let $P1 (-1, -2)$, $P2 (2, 4)$

$X_{min} = 0$, $X_{max} = 1$, $Y_{min} = 0$, $Y_{max} = 1$

- $dx = 2 - (-1) = 3$; $dy = 4 - (-2) = 6$
- $P1 = -dx = -3$; $q1 = x1 - X_{min} = -1 - 0 = -1$; $u_1 = q1 / P1 = 1/3$ Left
- $P2 = dx = 3$; $q2 = X_{max} - x1 = 1 - (-1) = 2$; $u_2 = q2 / P2 = 2/3$ Right
- $P3 = -dy = -6$; $q3 = y1 - Y_{min} = -2 - 0 = -2$; $u_3 = q3 / P3 = 1/3$ Bottom
- $P4 = dy = 6$; $q4 = Y_{max} - y1 = 1 - (-2) = 3$; $u_4 = q4 / P4 = 1/2$ Top
- for $(P_k < 0)$ $u'1 = \text{MAX}(1/3, 1/3, 0) = 1/3$
- for $(P_k > 0)$ $u'2 = \text{MIN}(2/3, 1/2, 1) = 1/2$ Since $u'1 < u'2$ there is a visible section

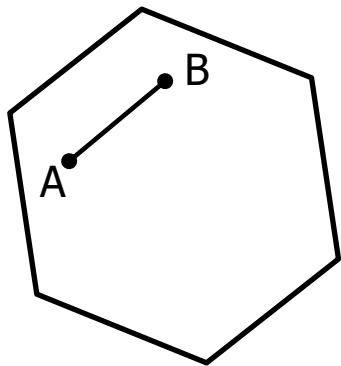
compute new endpoints

- $U'1 = 1/3$;
- $x1' = x1 + dx \cdot u'1 = -1 + (3 \cdot 1/3) = 0$
- $y1' = y1 + dy \cdot u'1 = -2 + (6 \cdot 1/3) = 0$
- $U'2 = 1/2$;
- $x2' = x1 + dx \cdot u'2 = -1 + (3 \cdot 1/2) = 1/2$
- $y2' = y1 + dy \cdot u'2 = -2 + (6 \cdot 1/2) = 1$

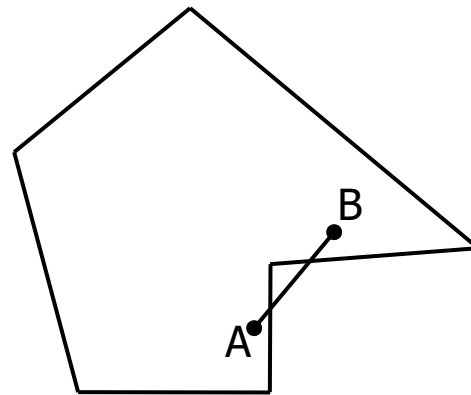


Polygon Clipping

- Convex Polygonal Clipping Windows:
 - A polygonal is called convex if the line joining any two interior points of the polygon lies completely inside the polygon
 - A non convex polygon is said to be concave



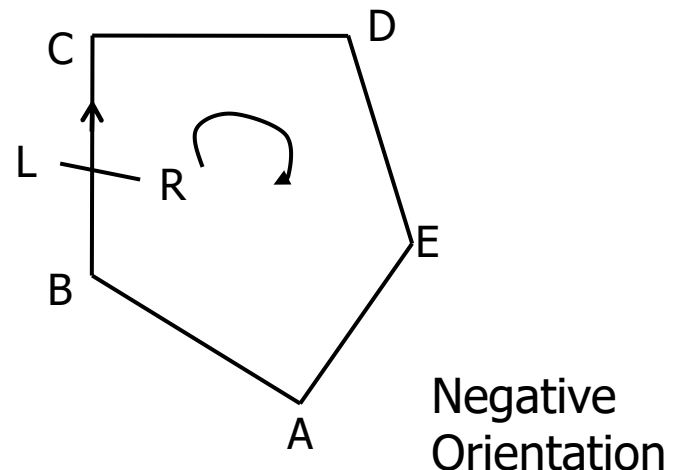
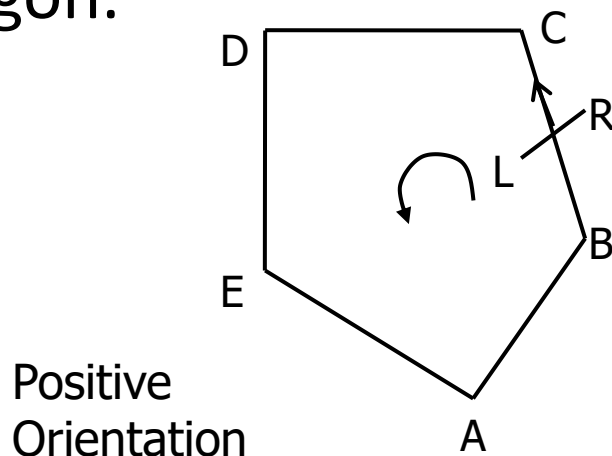
Convex Polygon



Concave Polygon

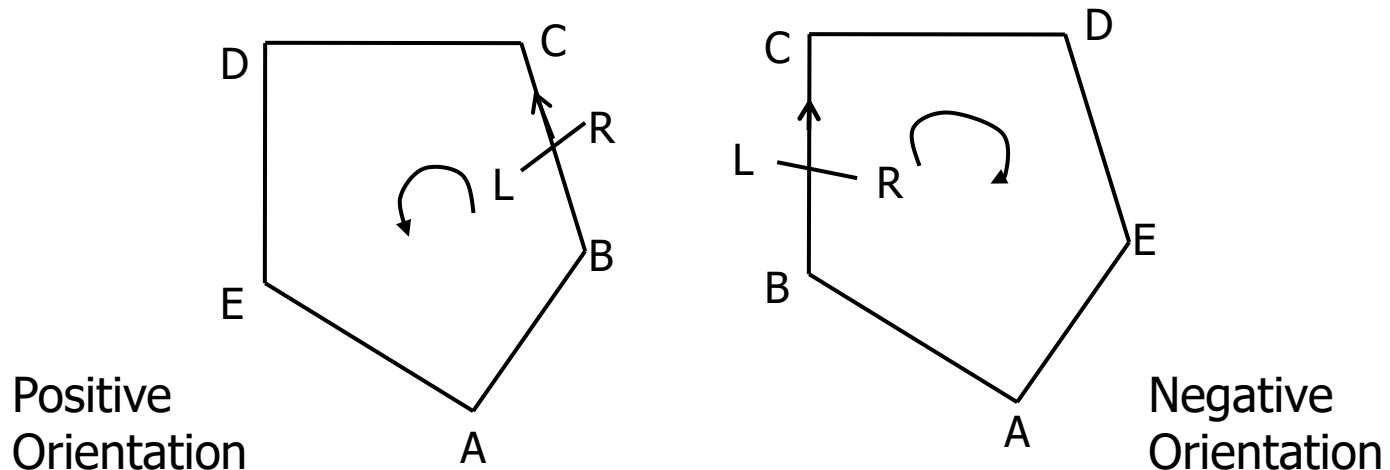
Polygon Clipping

- A Polygon with vertices $P_1 \dots P_N$ (and edges $P_i P_{i-1}$ and $P_1 P_N$) is said to be positively oriented if a tour of the vertices in the given order produces a counterclockwise circuit.
- The left hand of a person standing along any directed edge $P_i P_{i-1}$ or $P_1 P_N$ would be pointing inside the polygon.



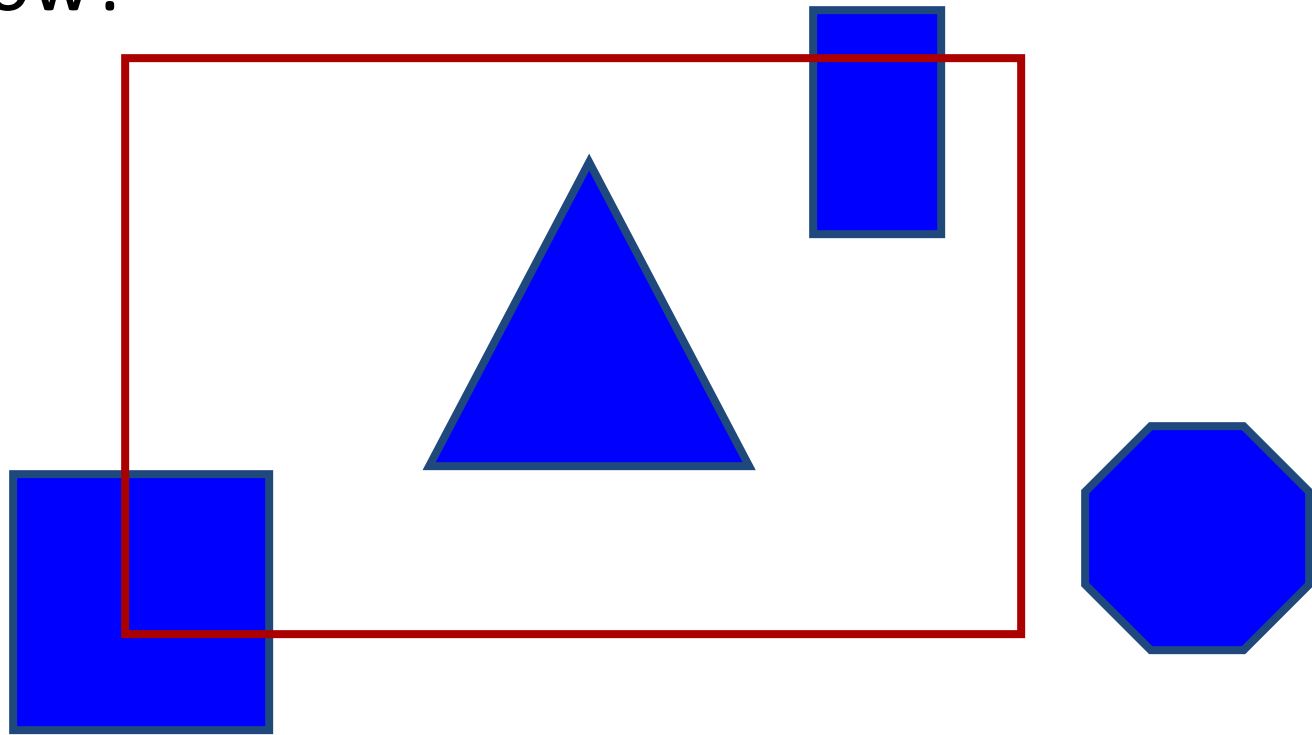
Polygon Clipping

- $A(x_1, y_1)$ and (x_2, y_2) be the end points of a directed line segment
- A point $p(x, y)$ will be to the left of the line segment if the expression $C = (x_2 - x_1)(y - y_1) - (y_2 - y_1)(x - x_1)$ is positive.
- The point is to the right of the line segment if this quantity is negative.
- If a point p is to the right of any one edge of a positively oriented, convex polygon, it is outside the polygon
- If it is to the left of every edge of the polygon, it is inside the polygon.



Polygon Clipping

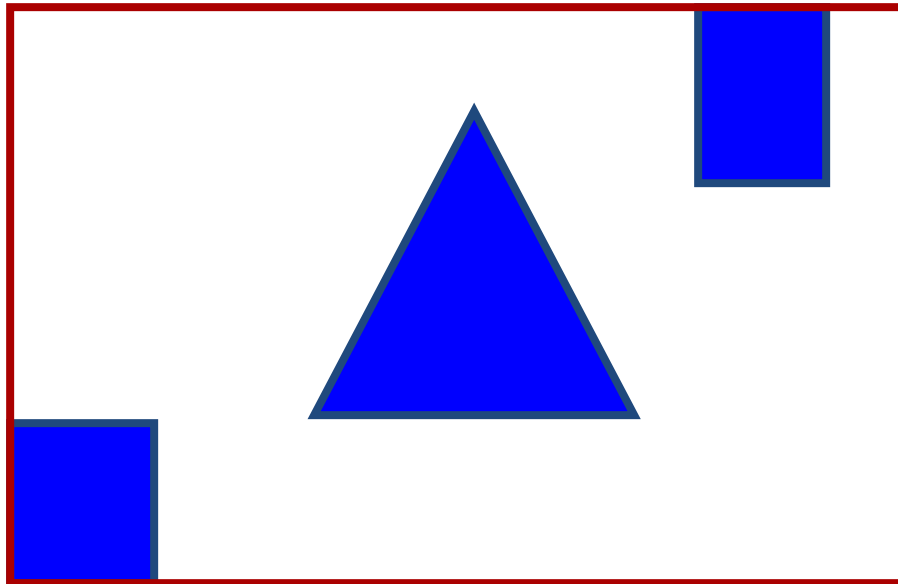
- Find the Part of a Polygon Inside the Clip Window?



Before Clipping

Polygon Clipping

- Find the Part of a Polygon Inside the Clip Window?



After Clipping

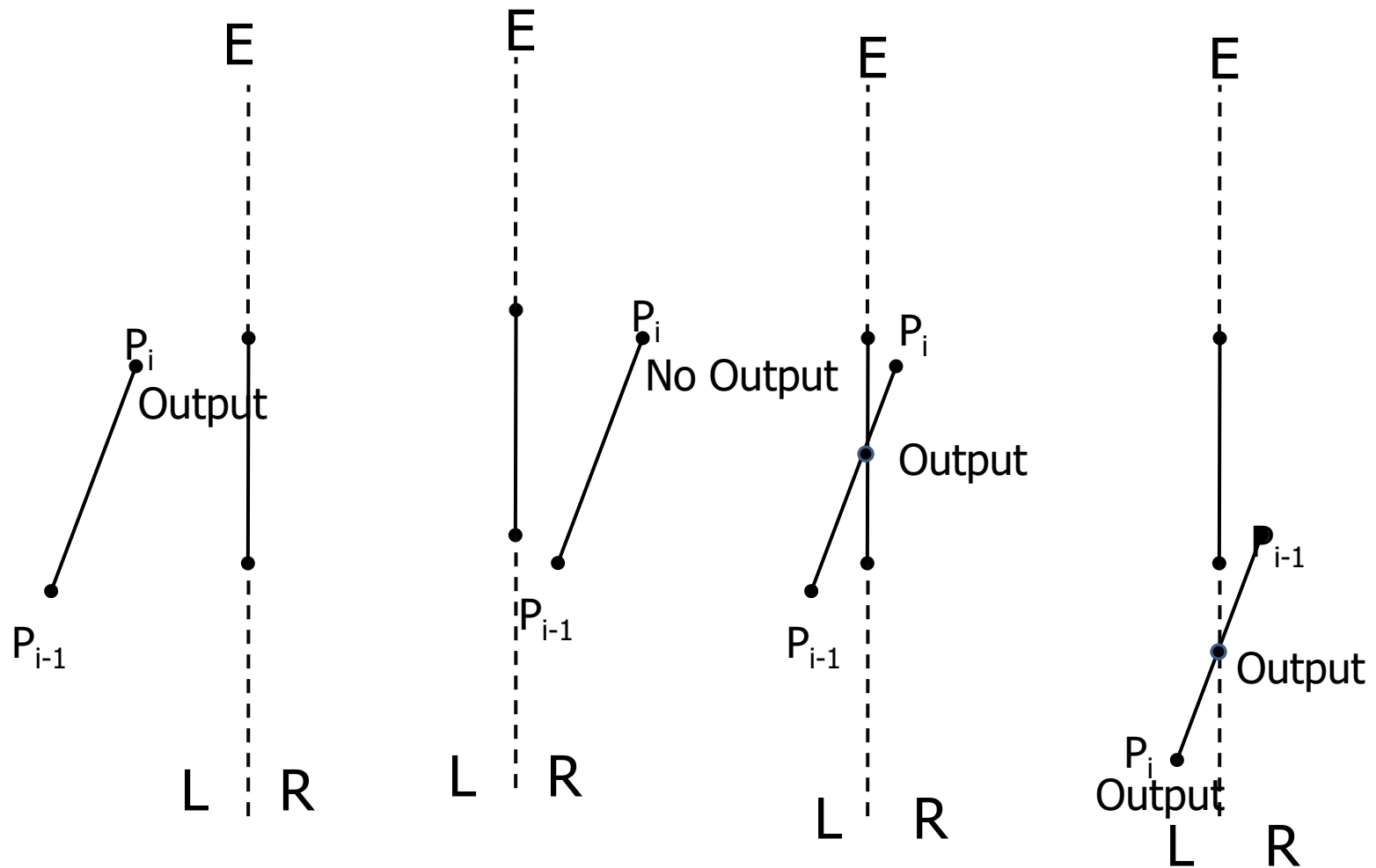
Sutherland-Hodgeman Polygon Clipping

- Let $P_1 \dots P_N$ be the vertex list of the polygon to be clipped. Let edge E , determined by endpoints A and B , be any edge of the positively oriented, convex clipping polygon.
- Clip each edge of the polygon in turn against the edge E of the clipping polygon, forming a new polygon whose vertices are determined as follows:

Sutherland-Hodgeman Polygon Clipping

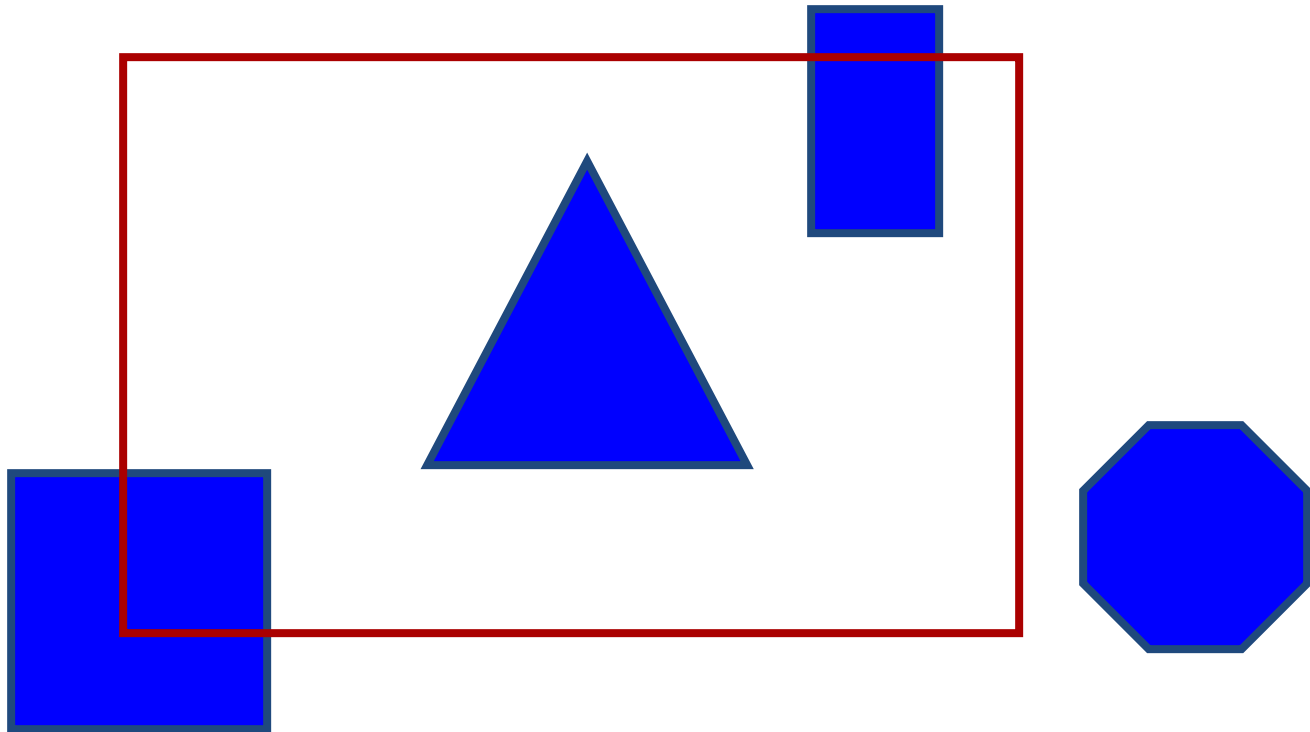
- Consider the edge $\overline{P_{i-1}P_i}$
- If both P_{i-1} and P_i are to the left of the edge, vertex P_i is placed on the vertex output list of the clipped polygon
- If both P_{i-1} and P_i are to the right of the edge, nothing is placed on the vertex output list of the clipped polygon
- If both P_{i-1} to the left and P_i is to the right of the edge E , the intersection point I of the line segment $\overline{P_{i-1}P_i}$ with the extended edge E is calculated and placed on the vertex output list.
- If both P_{i-1} to the right and P_i is to the left of the edge E , the intersection point I of the line segment $\overline{P_{i-1}P_i}$ with the extended edge E is calculated. Both I and P_i are placed on the vertex output list.

Sutherland-Hodgeman Polygon Clipping



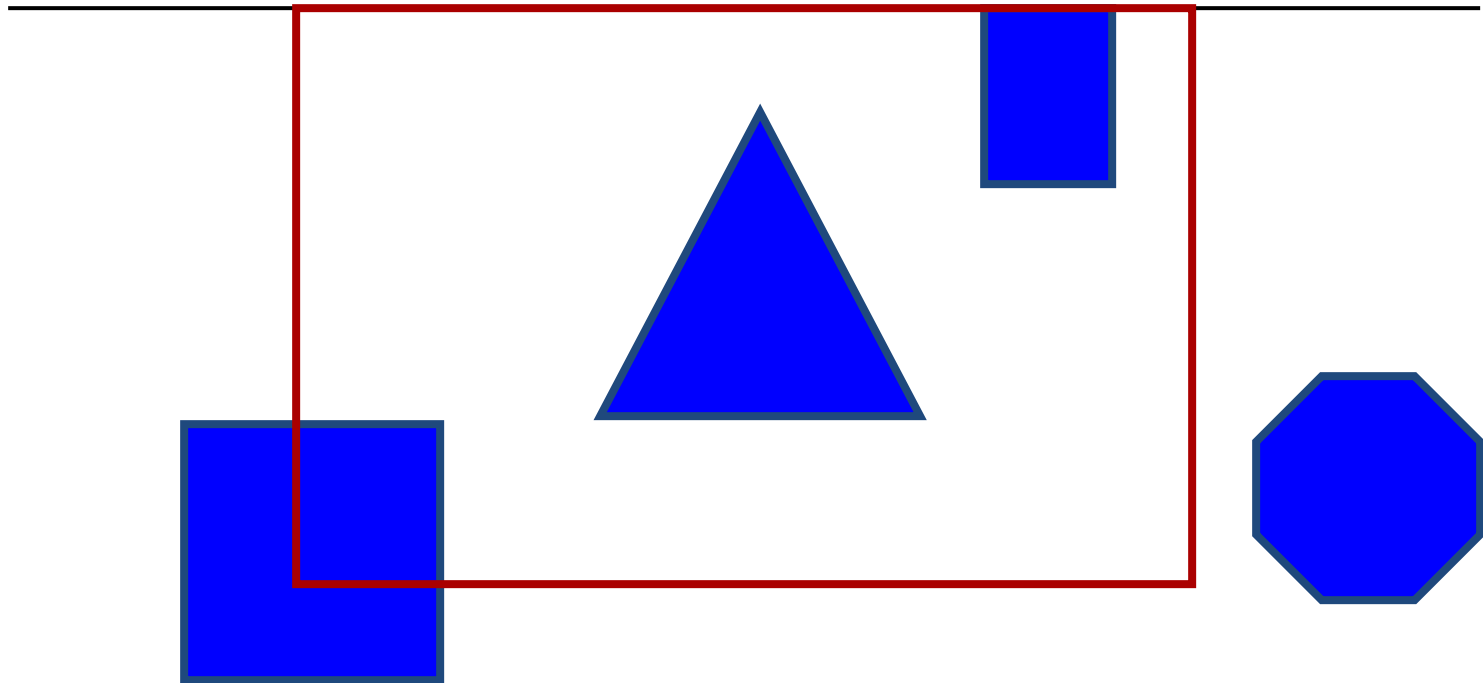
Sutherland-Hodgeman Polygon Clipping

- Clip to Each Window Boundary One at a Time



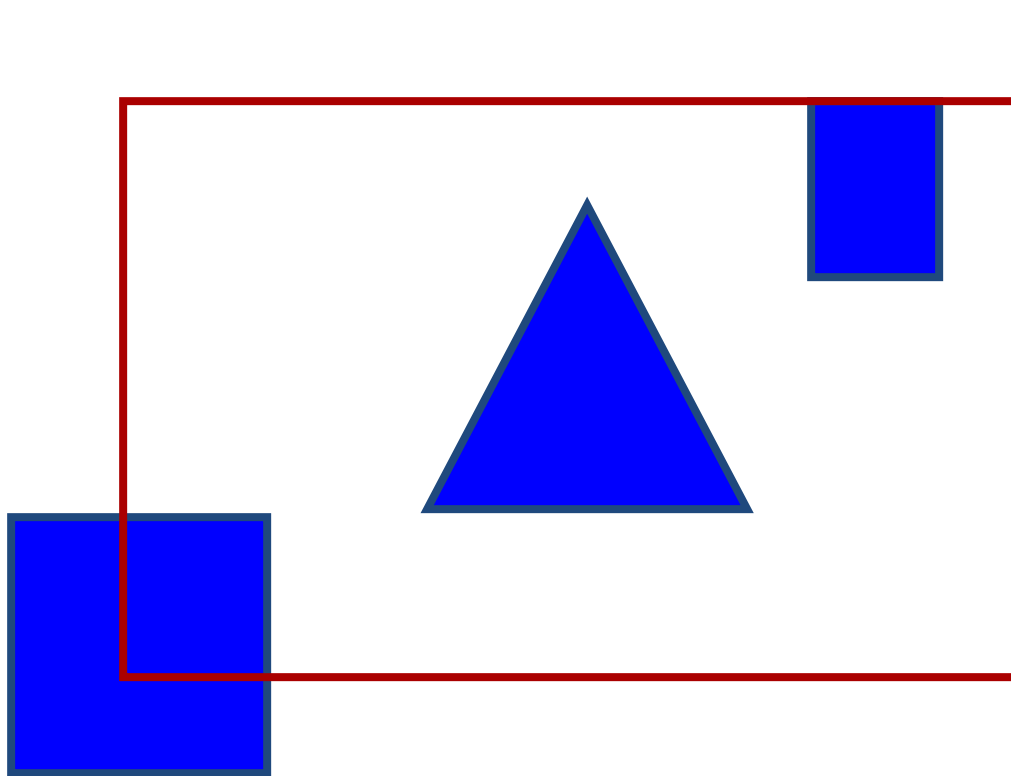
Sutherland-Hodgeman Polygon Clipping

- Clip to Each Window Boundary One at a Time



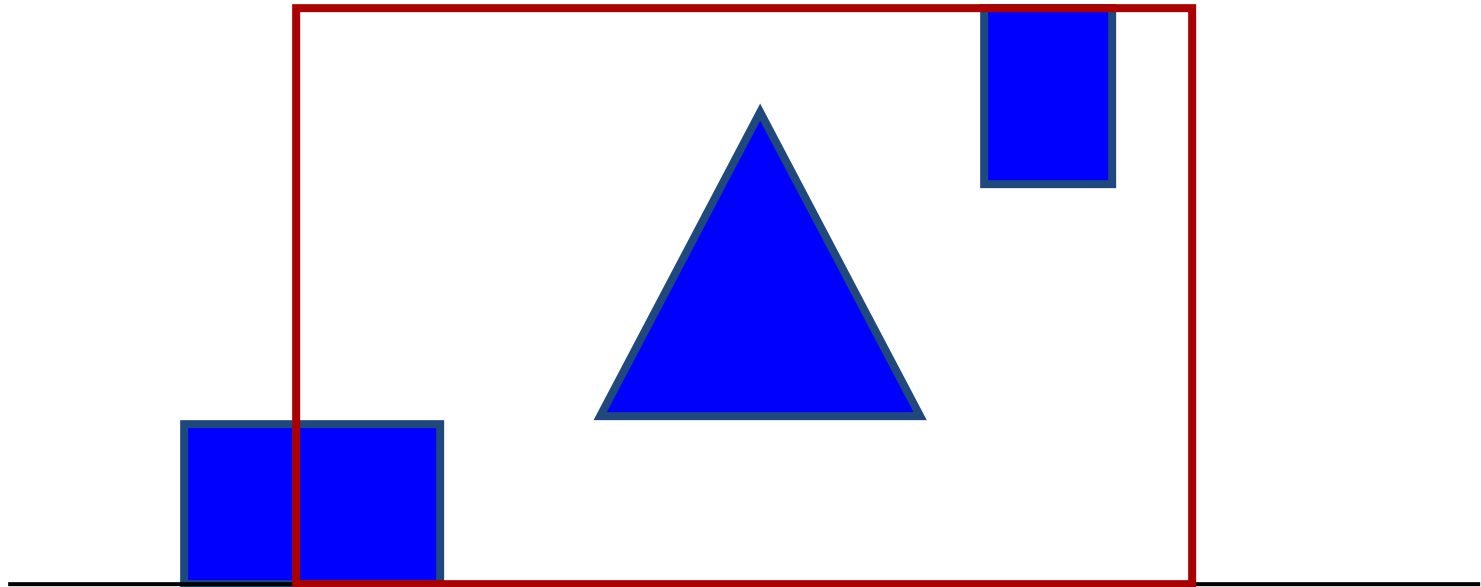
Sutherland-Hodgeman Polygon Clipping

- Clip to Each Window Boundary One at a Time



Sutherland-Hodgeman Polygon Clipping

- Clip to Each Window Boundary One at a Time



Sutherland-Hodgeman Polygon Clipping

- Clip to Each Window Boundary One at a Time

